

#### FLORIDA STATE UNIVERSITY COLLEGE OF MEDICINE

Research Workshop Series #5 Introduction to Biostatistics

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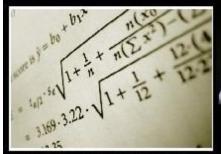


### Introduction



#### What is Statistics?

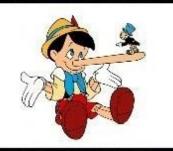
#### STATISTICIAN



What my friends think I do



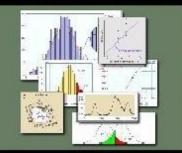
What my parents think I do



What society thinks I do



What my boss thinks I do



What I think I do



What I really do



### What is Statistics?

- "The goal of data analysis is simple to make the strongest possible conclusions from limited data.
- Statistics help you extrapolate from a particular set of data (sample) to make a more general conclusion (about the population)."
  - Motulsky, "Intuitive Biostatistics", Chapter 3





#### Parameter

- A parameter is a value of interest corresponding to a population.
  - Fixed
  - Unknown
- This is the answer we would like to know when we are designing a study
- We usually cannot find the exact value, because we rarely have complete information on all members of the population.



#### Statistic

- A **statistic** is the estimate of a parameter base on information contained in a **sample** 
  - Varies based on the sample taken
  - Can be calculated
- This is the answer we calculate from the study.
- If we did a different study, we would probably get a different statistic.
- We hope that this is a reasonable approximation of the parameter
  - But we have no way to know how close it is in any particular study



### **Example: Hypertension**

The NHANES (2011-2012) study estimated that 29.1% of the U.S. population suffers from hypertension in the U.S.

- This is a statistic based on a sample of members of the U.S. population
  - If we conducted another similar sample, we would have different participants and thus get a different estimate
- The parameter, the true proportion of the U.S. population that suffers from hypertension, is unknown.



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### **Popular Goals in Statistics**

#### **Descriptive Statistics**

- Reporting values (statistics) from the sample
- Different statistics to report for different types of data

#### Statistical Inference

- Estimation
  - Point (e.g. sample mean, sample proportion)
  - Interval (e.g. Confidence Intervals)
- Testing
  - Hypothesis Tests
- Modeling/Prediction
- All of these have <u>assumptions</u> that we should scrutinize!



### **Descriptive Statistics**



### **Types of Variables**

## You probably encounter data on a regular basis in your job

#### Can you think of some examples?



### **Types of Variables**

#### Categorical

- Binary
- Nominal
- Ordinal

#### Quantitative

- Count
- Continuous



### **Categorical Data**

#### Binary

- Two choices: Yes/No, Group A or B, etc.
- Example: Disease status, exposed/unexposed, gender

#### Nominal

- More than 2 choices with no inherent order
- Example: Blood type (A, B, AB, O)

#### Ordinal

- More than 2 choices with an inherent order
- Example: Pain level: None, mild, moderate, severe



#### **Quantitative Data**

#### Count Data

- Can take on many non-negative integer values (0, 1, 2, 3,...)
- Example: Number of Dental caries in a routine cleaning

#### Continuous Data

- Can take on any value within an interval
- Example: Blood Pressure, Height, Body mass index





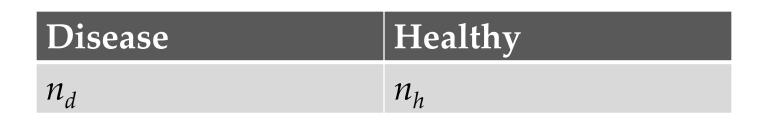


#### **Measures of Interest**

#### \*\*\*Depending on the kind of data you have, you would report different statistics to describe your data

#### **Measures for Categorical Data**

- For categorical data, the measures of interest are the *counts* or *proportions* of the observations that fall within a particular group
- We could report these in a short table, called a frequency distribution
  - Example: Number of patients with and without disease





# **Example Table:** (Beyerlein et al 2011)

"Table 1: Study characteristics of the data analyzed (n = 12,383)"

Excerpt: Child's Age (Among Smoking Mothers)

| Age         | Count | Percentage |
|-------------|-------|------------|
| 3–6 years   | 580   | 28.3       |
| 7–10 years  | 607   | 29.6       |
| 11–13 years | 415   | 20.3       |
| 14–17 years | 446   | 21.8       |



### Example

- Descriptive Statistics for Quantitative Data in Slade et al. 2011
- Table 5. Quantitative Measures of Symptom Experiences among 185 Cases with Temporomandibular Disorder (TMD)

| Measure  | Range | Ν   | Mean | SD   | Min | 5% | 25% | 50% | 75% | 95% | Max |
|--|-------|-----|------|------|-----|----|-----|-----|-----|-----|-----|
| Interference<br>in work due<br>to facial pain      | 10    | 185 | 2    | 2.6  | 0   | 0  | 0   | 1   | 3   | 8   | 10  |
| Number of<br>days kept<br>from usual<br>activities | 180   | 182 | 10.7 | 29.9 | 0   | 0  | 0   | 0   | 6   | 48  | 180 |



### **Descriptive Statistics**

#### Measures

| Categorical | Continuous                                   |
|-------------|--|
| Proportions | Location (Mean, Median, Mode)                |
| Counts      | Spread (Variance, SD, Quantiles, Range, IQR) |
|             | Other (coefficient of variation)             |

#### Graphical Displays

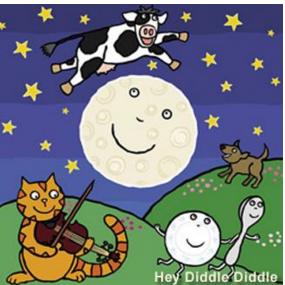
| Categorical | Continuous |
|-------------|------------|
| Bar Chart   | Histogram  |
| Pie Chart   | Boxplot    |



### Statistics Mnemonic

(Numeric Data)

"Hey, diddle diddle, The **median**'s the **middle** You add and divide for the **mean**. The **mode** is the one that appears the **most**. The **range** is the difference between."





### Estimation/Modeling



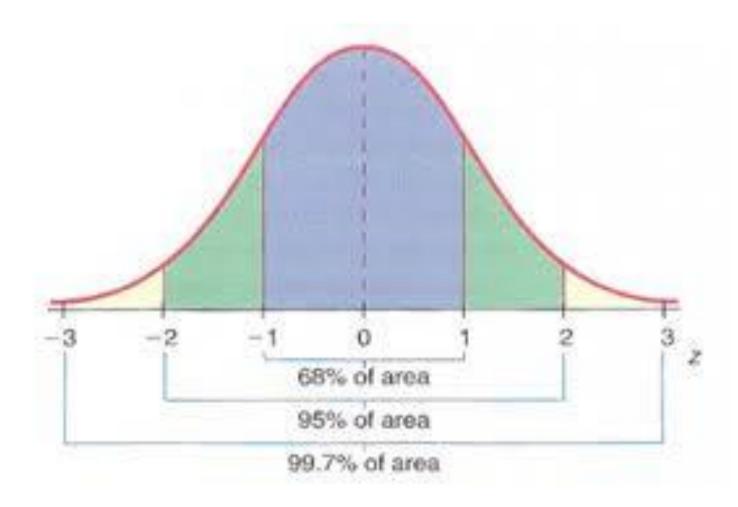
#### Background: Normal Distributions

- Normal distributions are everywhere in statistics and data analysis
- They form a special family of continuous distributions
- Properties:
  - Symmetric
  - Bell-shaped
  - Few extreme observations



#### **Normal Distributions**

#### Consider $Z \sim N(0,1)$





### Assumptions

- Before you conduct a statistical test, you MUST consider the assumptions of the test
  - What does the test assume?
  - What happens if the assumptions are violated?
  - Is this test appropriate for my data?
- Same holds if you run a model (and use the corresponding p-values)
- Same holds if you make a confidence interval

   Connection between tests and confidence
   intervals



#### **Statistical Tests Revisited**

Recall in Presentation 4, you had a handout called "Common Statistical Tests"

We will look at each item and carefully consider assumptions



### **Example: Statistical Tests**

- 1 sample:
  - Is my mean equal to a pre-specified number?
- 2 samples:
  - Are my two means equal?
- 3+ samples:
  - Are all three of my means equal



#### Review of Common Tests: Quantitative Data

| 1-Sample T-Test  | Indep. T-test  | Paired T-test  | ANOVA  |
|--|--|--|--|
| 1 quantitative<br>variable   | 2 independent<br>quantitative<br>variables                               | 2 dependent<br>quantitative<br>variables   | 3 or more<br>quantitative<br>variables                                   |
| Independent<br>observations  | Independent<br>observations<br>and samples                               | <b>Independent</b><br><b>pairs</b> of<br>observations (can<br>be related within<br>a pair) | Independent<br>observations<br>and samples                               |
| <b>Normally</b><br><b>distributed</b><br>population or a<br>large sample | <b>Normally</b><br><b>distributed</b><br>populations or<br>large samples | Normally<br>distributed<br>populations<br>(differences) or<br>large samples                | <b>Normally</b><br><b>distributed</b><br>populations,<br>equal variances |

Problem: Small non-normal samples!



#### Nonparametric Tests

- 1 sample:
  - Is my median equal to a pre-specified number?
- 2 samples:
  - Are my two medians equal?
- 3+ samples:
  - Are all three of my medians equal



#### **Review of Common Nonparametric Tests**

| Sign test   | Wilcoxon rank<br>sum (Mann-<br>Whitney)                                      | Wilcoxon sign-<br>rank  | Kruskal Wallis                             |
|---|--|---|--|
| 1 quantitative<br>variable or the<br>differences<br>between paired<br>quantitative<br>variables | 2 independent<br>quantitative<br>variables                                   | 2 dependent<br>quantitative<br>variables  | 3 or more<br>quantitative<br>variables     |
| Independent<br>observations   | At least 8<br>Independent<br>observations,<br>and<br>independent<br>samples, | At least 6<br><b>Independent</b><br><b>observations</b> ,<br>Assumes the<br>difference<br>between the<br>variables is<br><b>symmetric</b> ! | Independent<br>observations<br>and samples |



#### **Correlation Tests**

- Pearson:
  - Are my two variables linearly related with a nonzero slope?
    - Yes, this is equivalent to testing the slope in a simple linear regression model (coming up)
- Spearman:
  - Are the ranks of the values of my two variables linearly related?
  - i.e. Are my two variables increasing or decreasing together?



#### Review of Common Correlation Tests

| Pearson  | Spearman                                      |
|--|---|
| 2 continuous variables   | 2 continuous or ordinal<br>variables          |
| <b>Independent pairs</b> of<br><b>normally distributed</b><br>observations,<br>variables are <b>linearly</b><br><b>related</b> | At least 5 <b>Independent</b><br><b>pairs</b> |



### **Tests for Categorical Data**

- 1 sample:
  - Are the proportions of observations for each possibility consistent with my initial guess?
- 2 samples:
  - Are the proportions of each possibility equal in two different samples?



#### Review of Common Tests: Categorical Data

| Chi Square<br>Goodness of fit  | Chi Square<br>Indep.   | Fisher's Exact<br>Test                  |
|--|--|---|
| 1 Categorical<br>Variable  | 2 (or more)<br>Categorical<br>variables  | 2 (or more)<br>categorical<br>variables |
| <b>Independent</b><br><b>observations</b> ,<br>at least 5-10<br>expected in all<br>cells | <b>Independent</b><br><b>observations</b> ,<br>at least 5-10<br>expected in all<br>cells | Independent<br>Observations             |



### Linear Regression

- Simple
  - If I made a scatterplot based on my 2 variables, and drew a line through all the points, would that line be horizontal?
- Multiple
  - Similar interpretation, between outcome and each predictor, holding all others constant



### **Review of Linear Regression**

| Simple   | Multiple   |
|--|--|
| 1 continuous outcome, 1<br>continuous predictor  | 1 continuous outcome, 1 or<br>more predictors (they can be<br>continuous, nominal or<br>ordinal)   |
| <pre>pairs of observations,<br/>variables are linearly related,<br/>errors (residuals) are<br/>normally distributed and<br/>independent,<br/>predictor is measured<br/>precisely</pre> | groups of observations,<br>outcome is linearly related to<br>the predictors,<br>errors (residuals) are<br>normally distributed and<br>independent,<br>predictors are measured<br>precisely and not linearly<br>related to each other |



#### The Importance of Proper Sampling and Analysis

- The way the sample is selected (i.e. the study design), determines if the results are valid!
- Bad study designs yield bad results, may give misleading conclusions, and results from the sample are not generalizable to the population
- Similarly, inappropriate statistical analyses yield invalid conclusions.
- "Garbage in, garbage out!"



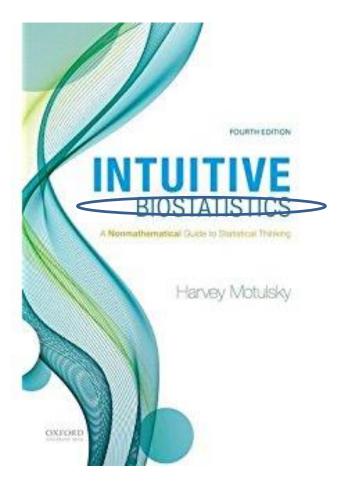


### **Choose Statistics Wisely**

- Many analyses are possible, but only a few make sense
- Always look at graphs to visualize your data!
- Always critically evaluate assumptions
- Always consider the broader picture to make sure you are doing analyses that make sense



### **Recommended Reading**



- Excellent reference
- Not a traditional stats text book
- Paperback
- Words, not numbers
- Just concepts



### Thank you!

### Questions & Discussion